

### Gabarito – 1

$$\begin{aligned} 1. & (2^3) \cdot (2^2) \\ & = 2^{3+2} \\ & = 2^5 \\ & = 32 \end{aligned}$$

$$\begin{aligned} 2. & (5^4) \div (5^2) \\ & = 5^{4-2} \\ & = 5^2 \\ & = 25 \end{aligned}$$

$$\begin{aligned} 3. & (6^2) \cdot (6^3) \\ & = 6^{2+3} \\ & = 6^5 \\ & = 7776 \end{aligned}$$

$$\begin{aligned} 4. & (3^5) \div (3^2) \\ & = 3^{5-2} \\ & = 3^3 \\ & = 27 \end{aligned}$$

$$\begin{aligned} 5. & (2^6) \div (2^3) \\ & = 2^{6-3} \\ & = 2^3 \\ & = 8 \end{aligned}$$

$$\begin{aligned} 6. & (3^2)^3 \\ & = 3^{2 \cdot 3} \\ & = 3^6 \\ & = 729 \end{aligned}$$

$$\begin{aligned} 7. & (2^3)^2 \\ & = 2^{3 \cdot 2} \\ & = 2^6 \\ & = 64 \end{aligned}$$

$$\begin{aligned} 8. & (5^2)^2 \\ & = 5^{2 \cdot 2} \\ & = 5^4 \\ & = 625 \end{aligned}$$

$$\begin{aligned} 9. & (4^1)^3 \\ & = 4^{1 \cdot 3} \\ & = 4^3 \\ & = 64 \end{aligned}$$

$$\begin{aligned} 10. & (2^2)^4 \\ & = 2^{2 \cdot 4} \\ & = 2^8 \\ & = 256 \end{aligned}$$

$$\begin{aligned} 11. & [2^2 \cdot 3]^2 \\ & = [4 \cdot 3]^2 \\ & = 12^2 \\ & = 144 \end{aligned}$$

$$\begin{aligned} 12. & [4 \cdot (2^2)]^2 \\ & = [4 \cdot 4]^2 \\ & = 16^2 \end{aligned}$$

$$\begin{aligned} &= 256 \\ 13. & [3 \cdot (3^2)]^2 \\ &= [3 \cdot 9]^2 \\ &= 27^2 \\ &= 729 \\ 14. & [(2^2) \cdot (2^3)] \div 2^4 \\ &= 2^{2+3} \div 2^4 \\ &= 2^5 \div 2^4 \\ &= 2^{5-4} \\ &= 2 \\ 15. & [(2^3) \cdot (5^3)] \div 10^2 \\ &= (8 \cdot 125) \div 100 \\ &= 1000 \div 100 \\ &= 10 \\ 16. & (7^0) \cdot 5 \\ &= 1 \cdot 5 \\ &= 5 \\ 17. & (8^0) + (5^0) \\ &= 1 + 1 \\ &= 2 \\ 18. & (2^0) \cdot (7^2) \\ &= 1 \cdot 49 \\ &= 49 \\ 19. & (3^3) \cdot (3^0) \\ &= 27 \cdot 1 \\ &= 27 \\ 20. & (9^0) \cdot (4^2) \\ &= 1 \cdot 16 \\ &= 16 \\ 21. & (2^4) \div (2^6) \\ &= 2^{4-6} \\ &= 2^{-2} \\ &= \frac{1}{2^2} \\ &= \frac{1}{4} \\ 22. & (5^3) \cdot (5^{-1}) \\ &= 5^{3-1} \\ &= 5^2 \\ &= 25 \\ 23. & (4^5) \div (4^7) \\ &= 4^{5-7} \\ &= 4^{-2} \\ &= \frac{1}{4^2} \\ &= \frac{1}{16} \\ 24. & (10^3) \div (10^5) \\ &= 10^{3-5} \end{aligned}$$

$$\begin{aligned}
&= 10^{-2} \\
&= \frac{1}{10^2} \\
&= \frac{1}{100} \\
25. &(2^{-2}) \cdot (2^5) \\
&= 2^{-2+5} \\
&= 2^3 \\
&= 8 \\
26. &(10^2) \div (10) \\
&= 10^2 \div 10^1 \\
&= 10^{2-1} \\
&= 10 \\
27. &(9^2) \div (3^2) \\
&= \left(\frac{9}{3}\right)^2 \\
&= 3^2 \\
&= 9 \\
28. &(12^2) \div (6^2) \\
&= \left(\frac{12}{6}\right)^2 \\
&= 2^2 \\
&= 4 \\
29. &(8^2) \div (2^2) \\
&= \left(\frac{8}{2}\right)^2 \\
&= 4^2 \\
&= 16 \\
30. &[(6^2) \div 6]^2 \\
&= [36 \div 6]^2 \\
&= 6^2 \\
&= 36
\end{aligned}$$

**Gabarito – 2**

1.
$$\begin{aligned}
&[(8 + 4) \div 2] + 3 \\
&12 \div 2 + 3 \\
&6 + 3 = 9
\end{aligned}$$
2.
$$\begin{aligned}
&[5 + 3^2] \cdot 2 \\
&[5 + 9] \cdot 2 \\
&14 \cdot 2 = 28
\end{aligned}$$
3.
$$\begin{aligned}
&(6^2 \div 3) + 1 \\
&36 \div 3 + 1 \\
&12 + 1 = 13
\end{aligned}$$
4.
$$\begin{aligned}
&[8 + 2^3] \div 4 \\
&[8 + 8] \div 4 \\
&16 \div 4 = 4
\end{aligned}$$

5.  $(10 - 2^2) + 5$   
 $(10 - 4) + 5$   
 $6 + 5 = 11$
6.  $(3^3 - 7) + 2$   
 $(27 - 7) + 2$   
 $20 + 2 = 22$
7.  $4 \cdot (2^2 + 1)$   
 $4 \cdot (4 + 1)$   
 $4 \cdot 5 = 20$
8.  $(18 \div 3^2) + 6$   
 $(18 \div 9) + 6$   
 $2 + 6 = 8$
9.  $7 + (5^2 - 10)$   
 $7 + (25 - 10)$   
 $7 + 15 = 22$
10.  $(2^4 \div 4) + 9$   
 $(16 \div 4) + 9$   
 $4 + 9 = 13$
11.  $[3 + 2^3]^2$   
 $[3 + 8]^2$   
 $11^2 = 121$
12.  $(12 \div 2) + 2^2$   
 $6 + 4 = 10$
13.  $9 - (3^2 - 1)$   
 $9 - (9 - 1)$   
 $9 - 8 = 1$
14.  $(5^2 \div 5) + 8$   
 $(25 \div 5) + 8$   
 $5 + 8 = 13$
15.  $6 + (2 \cdot 3^2)$   
 $6 + (2 \cdot 9)$   
 $6 + 18 = 24$
16.  $(16 \div 2^2) + 7$   
 $(16 \div 4) + 7$   
 $4 + 7 = 11$
17.  $10 + (2^3 \div 2)$   
 $10 + (8 \div 2)$   
 $10 + 4 = 14$
18.  $(4^2 + 6) \div 2$   
 $(16 + 6) \div 2$   
 $22 \div 2 = 11$
19.  $[15 - 3^2] + 4$   
 $[15 - 9] + 4$   
 $6 + 4 = 10$
20.  $(2^5 \div 8) + 3$   
 $(32 \div 8) + 3$   
 $4 + 3 = 7$
21.  $[(2^3 + 4^2) \div 4] + 3^2$   
 $[(8 + 16) \div 4] + 9$

- $$24 \div 4 + 9$$
- $$6 + 9 = 15$$
22.  $[18 - (2^3 + 3)] + [2^2 \cdot 3]$   
 $[18 - (8 + 3)] + [4 \cdot 3]$   
 $[18 - 11] + 12$   
 $7 + 12 = 19$
23.  $[(5^2 - 9) \cdot 2] + 2^3$   
 $[(25 - 9) \cdot 2] + 8$   
 $16 \cdot 2 + 8$   
 $32 + 8 = 40$
24.  $[24 \div (2^2 + 2)] + 3^3$   
 $[24 \div (4 + 2)] + 27$   
 $24 \div 6 + 27$   
 $4 + 27 = 31$
25.  $[(4^2 + 2^3) \div 2] + [3^2 - 1]$   
 $[(16 + 8) \div 2] + [9 - 1]$   
 $24 \div 2 + 8$   
 $12 + 8 = 20$
26.  $[30 - (3^2 + 5)] \cdot 2$   
 $[30 - (9 + 5)] \cdot 2$   
 $[30 - 14] \cdot 2$   
 $16 \cdot 2 = 32$
27.  $[(2^5 \div 4) + (5^2 \div 5)] \cdot 2$   
 $[(32 \div 4) + (25 \div 5)] \cdot 2$   
 $[8 + 5] \cdot 2$   
 $13 \cdot 2 = 26$
28.  $[40 \div (2^3 + 2)] + [(3^2) \cdot 2]$   
 $[40 \div (8 + 2)] + [9 \cdot 2]$   
 $40 \div 10 + 18$   
 $4 + 18 = 22$
29.  $[(6^2 - 20) \div 4] + [(2^3 + 1)]$   
 $[(36 - 20) \div 4] + [8 + 1]$   
 $16 \div 4 + 9$   
 $4 + 9 = 13$
30.  $[(3^3 + 5^2) \div 4] + [(2^4 \div 2)]$   
 $[(27 + 25) \div 4] + [16 \div 2]$   
 $52 \div 4 + 8$   
 $13 + 8 = 21$

Gabarito 3

## 1) Calcule as potências

- a)  $2^3 = 8$   
b)  $5^2 = 25$   
c)  $10^3 = 1000$   
d)  $4^3 = 64$   
e)  $6^2 = 36$   
f)  $3^4 = 81$

- g)  $7^2 = 49$
- h)  $8^2 = 64$
- i)  $9^3 = 729$
- j)  $2^5 = 32$

## 2) Potências com bases negativas

- a)  $(-2)^3 = -8$
- b)  $(-3)^2 = 9$
- c)  $(-4)^3 = -64$
- d)  $(-5)^2 = 25$
- e)  $(-2)^4 = 16$

## 3) Expoente negativo

- a)  $4^{-2} = \frac{1}{16}$
- b)  $4^{-3} = \frac{1}{64}$
- c)  $5^{-1} = \frac{1}{5}$
- d)  $3^{-3} = \frac{1}{27}$
- e)  $10^{-2} = \frac{1}{100}$
- f)  $10^{-3} = \frac{1}{1000}$
- g)  $2^{-5} = \frac{1}{32}$
- h)  $7^{-1} = \frac{1}{7}$
- i)  $1^{-18} = 1$

## 4) Propriedades da potência

- a)  $2^3 \cdot 2^4 = 2^7 = 128$
- b)  $5^2 \cdot 5^3 = 5^5 = 3125$
- c)  $10^5 \div 10^2 = 10^3 = 1000$
- d)  $3^6 \div 3^2 = 3^4 = 81$
- e)  $(2^3)^2 = 2^6 = 64$
- f)  $(5^2)^3 = 5^6 = 15625$
- g)  $4^3 \cdot 4^2 = 4^5 = 1024$
- h)  $6^5 \div 6^3 = 6^2 = 36$
- i)  $(3^2)^4 = 3^8 = 6561$

j)  $7^3 \cdot 7^0 = 7^3 = 343$

k)  $(2 \cdot 3)^2 = 6^2 = 36$

l)  $(4 \cdot 5)^2 = 20^2 = 400$

m)  $(6 \cdot 2)^3 = 12^3 = 1728$

n)  $(10 \div 2)^2 = 5^2 = 25$

o)  $(12 \div 3)^3 = 4^3 = 64$

## 5) Potências de base 10

a)  $10^2 = 100$

b)  $10^4 = 10000$

c)  $10^0 = 1$

d)  $10^{-1} = \frac{1}{10}$

e)  $10^{-2} = \frac{1}{100}$

f)  $10^{-4} = \frac{1}{10000}$

## 6) Problemas

a)  
A bactéria dobra a cada hora:

$$2^5 = 32$$

Resposta: **32 bactérias**

b)  
 $x^2 = 81$

$$x = 9 \text{ ou } x = -9$$

Resposta: **9 ou -9**

c)  
Lado:

$$3^2 = 9$$

Área do quadrado:

$$9^2 = 81$$

Resposta: **81 m<sup>2</sup>**

## 7) Potenciação de frações

a)  $\left(\frac{2}{3}\right)^2 = \frac{4}{9}$

b)  $\left(\frac{4}{7}\right)^2 = \frac{16}{49}$

c)  $\left(\frac{7}{5}\right)^2 = \frac{49}{25}$

d)  $\left(\frac{1}{3}\right)^2 = \frac{1}{9}$

e)  $\left(\frac{5}{3}\right)^2 = \frac{25}{9}$

f)  $\left(\frac{7}{30}\right)^0 = 1$

g)  $\left(\frac{9}{5}\right)^1 = \frac{9}{5}$

h)  $\left(\frac{2}{3}\right)^3 = \frac{8}{27}$

i)  $\left(\frac{1}{5}\right)^3 = \frac{1}{125}$

j)  $\left(\frac{1}{2}\right)^2 = \frac{1}{4}$

k)  $\left(\frac{2}{3}\right)^4 = \frac{16}{81}$

l)  $\left(\frac{2}{5}\right)^1 = \frac{2}{5}$

m)  $\left(\frac{3}{11}\right)^2 = \frac{9}{121}$

n)  $\left(\frac{9}{4}\right)^0 = 1$

o)  $\left(\frac{12}{13}\right)^2$

$$\begin{aligned}\left(\frac{12}{13}\right)^2 &= \frac{12^2}{13^2} \\ &= \frac{144}{169}\end{aligned}$$

## 8) Resolva as expressões numéricas

a)

$$2 + 8 - 3 - 5 + 15$$

$$10 - 3 - 5 + 15$$

$$7 - 5 + 15$$

$$2 + 15 = 17$$

b)

$$12 + [35 - (10 + 2) + 2]$$

$$12 + [35 - 12 + 2]$$

$$12 + [23 + 2]$$

$$12 + 25 = 37$$

c)

$$[(18 + 3 \cdot 2) \div 8 + 5 \cdot 3] \div 6$$

$$[(18 + 6) \div 8 + 15] \div 6$$

$$[24 \div 8 + 15] \div 6$$

$$[3 + 15] \div 6$$

$$18 \div 6 = 3$$

d)

$$37 + [-25 - (-11 + 19 - 4)]$$

$$37 + [-25 - (8 - 4)]$$

$$37 + [-25 - 4]$$

$$37 + (-29)$$

$$= 8$$

**e)**

$$60 \div \{2 \cdot [-7 + 18 \div (-3 + 12)]\} - [7 \cdot (-3) - 18 \div (-2) + 1]$$

$$60 \div \{2 \cdot [-7 + 18 \div 9]\} - [-21 - (-9) + 1]$$

$$60 \div \{2 \cdot [-7 + 2]\} - [-21 + 9 + 1]$$

$$60 \div \{2 \cdot (-5)\} - [-11]$$

$$60 \div (-10) + 11$$

$$-6 + 11 = 5$$

**f)**

$$-8 + \{-5 + [(8 - 12) + (13 + 12)] - 10\}$$

$$-8 + \{-5 + [(-4) + 25] - 10\}$$

$$-8 + \{-5 + 21 - 10\}$$

$$-8 + 6 = -2$$

**g)**

$$3 - \{2 + (11 - 15) - [5 + (-3 + 1)] + 8\}$$

$$3 - \{2 + (-4) - [5 - 2] + 8\}$$

$$3 - \{2 - 4 - 3 + 8\}$$

$$3 - \{3\}$$

$$= 0$$

**h)**

$$[-1 + (2^2 - 5 \cdot 6)] \div (-5 + 2) + 1$$

$$[-1 + (4 - 30)] \div (-3) + 1$$

$$[-1 - 26] \div (-3) + 1$$

$$-27 \div (-3) + 1$$

$$9 + 1 = 10$$

**i)**

$$[\sqrt{100} - (2^4 - 8) \cdot 2 - 24] \div [2^2 - (-3 + 2)]$$

$$[10 - (16 - 8) \cdot 2 - 24] \div [4 - (-1)]$$

$$[10 - 8 \cdot 2 - 24] \div 5$$

$$[10 - 16 - 24] \div 5$$

$$-30 \div 5 = -6$$

**j)**

$$\{[(8 \cdot 4 + 3) \div 7 + (3 + 15 \div 5) \cdot 3] \cdot 2 - (19 - 7) \div 6\} \cdot 2 + 12$$

$$\{[(32 + 3) \div 7 + (3 + 3) \cdot 3] \cdot 2 - 12 \div 6\} \cdot 2 + 12$$

$$\{[35 \div 7 + 6 \cdot 3] \cdot 2 - 2\} \cdot 2 + 12$$

$$\{[5 + 18] \cdot 2 - 2\} \cdot 2 + 12$$

$$\{23 \cdot 2 - 2\} \cdot 2 + 12$$

$$\{46 - 2\} \cdot 2 + 12$$

$$44 \cdot 2 + 12$$

$$88 + 12 = 100$$

## 9) Calcule o valor das expressões

**1)**

$$\frac{4}{5} \cdot (3 + 0,4) - 3,21$$

$$\frac{4}{5} \cdot 3,4 - 3,21$$

$$2,72 - 3,21 = -0,49$$

**2)**

$$\frac{4}{3} + \frac{7}{5} \cdot \left(\frac{1}{2} + \frac{4}{9}\right) - \frac{1}{5}$$

$$\frac{4}{3} + \frac{7}{5} \cdot \frac{17}{18} - \frac{1}{5}$$

$$\frac{4}{3} + \frac{119}{90} - \frac{1}{5}$$

$$\frac{120}{90} + \frac{119}{90} - \frac{18}{90}$$

$$\frac{221}{90}$$

**3)**

$$\frac{\frac{4}{5} \cdot \left(\frac{7}{3} - 1\right)}{\frac{2}{9} - 3}$$

$$\frac{\frac{4}{5} \cdot \frac{4}{3}}{\frac{2}{9} - \frac{27}{9}}$$

$$\frac{\frac{16}{15}}{-\frac{25}{9}}$$

$$\frac{16 \cdot 9}{15 \cdot -25}$$

$$\frac{144}{-375}$$

$$-\frac{48}{125}$$

**Gabarito 4**

**1) Reduza a uma só potência**

a)  $(2^{15}) : (2^{10})$

$$2^{15-10} = 2^5$$

b)  $3 \cdot 3^2$

$$3^1 \cdot 3^2 = 3^3$$

c)  $[(-5)^6] : [(-5)^4]$

$$(-5)^{6-4} = (-5)^2$$

$$d) [(-7)^8]:[(-7)^2]$$

$$(-7)^{8-2} = (-7)^6$$

$$e) (2^{10}): (2^3)$$

$$2^{10-3} = 2^7$$

$$f) (-3)^2 \cdot (-3)^3$$

$$(-3)^{2+3} = (-3)^5$$

$$g) [(-2)^6] \cdot (-2)$$

$$(-2)^6 \cdot (-2)^1 = (-2)^7$$

$$h) 3^{-6} \cdot 3^2$$

$$3^{-6-2} = 3^{-8}$$

$$i) 2^8 \cdot 2^{-9}$$

$$2^{8-9} = 2^{-1}$$

$$j) 5^3 : 5^4$$

$$5^{3-4} = 5^{-1}$$

## 2) Potenciações com expoentes negativos

$$a) 4^{-2}$$

$$= \frac{1}{4^2} = \frac{1}{16}$$

$$b) (-3)^{-1}$$

$$= \frac{1}{-3} = -\frac{1}{3}$$

$$\text{c) } (-5)^{-2}$$

$$= \frac{1}{(-5)^2} = \frac{1}{25}$$

d)

$$\left(\frac{3}{4}\right)^2 = \frac{9}{16}$$

$$\frac{1}{\frac{9}{16}}$$

$$1 \cdot \frac{16}{9}$$

$$= \frac{16}{9}$$

$$\text{e) } \left(1\frac{1}{2}\right)^{-3}$$

$$\left(\frac{3}{2}\right)^{-3}$$

$$= \left(\frac{2}{3}\right)^3$$

$$= \frac{8}{27}$$

### 3) Calcule as potências

$$\text{a) } \left(-\frac{1}{3}\right)^4 =$$

$$= \frac{(-1)^4}{3^4}$$

$$= \frac{1}{81}$$

$$\text{b) } (0,2)^3$$

$$0,2 \cdot 0,2 \cdot 0,2 = 0,008$$

$$\text{c) } \left(-\frac{3}{5}\right)^0 = \\ = 1$$

$$\text{d) } (-1)^5 \\ = -1$$

$$\text{e) } \left(-\frac{1}{2}\right)^4 = \\ = \frac{1}{16}$$

$$\text{f) } \left(\frac{2}{3}\right)^3 \\ = \frac{8}{27}$$

$$\text{g) } (-0,5)^1 \\ = -0,5$$

$$\text{h) } (0,03)^3 \\ 0,03 \cdot 0,03 \cdot 0,03 = 0,00027$$

#### **4) Determine o valor das expressões**

$$\text{a) } (-8) : (-8) \\ = 1$$

$$\text{b) } 25 : (-5) \\ = -5$$

$$\text{c) } (-4)^2 + 16 - (-1) \\ 16 + 16 + 1 = 33$$

$$\text{d) } -8 \cdot 9 - (-10) \cdot 1 \\ -72 - (-10) = -72 + 10 = -62$$

$$e) 36:9 - (-1) \cdot (-8)$$

$$4 - 8 = -4$$

$$f) \{[16 + 3(9 - 1)]: [-8 + 3 \cdot 4]\}$$

$$\{[16 + 3 \cdot 8]: [-8 + 12]\}$$

$$\{[16 + 24]: 4\}$$

$$40:4 = 10$$

$$g) \left(-\frac{2}{3}\right)^3 + 1 =$$

$$-\frac{8}{27} + 1$$

$$= \frac{-8 + 27}{27} = \frac{19}{27}$$

$$h) (-8) - 1 + 9 - (-32)$$

$$-9 + 9 + 32 = 32$$

$$i) 16 + 3^5$$

$$16 + 243 = 259$$

$$j) 5^3 - 2^5$$

$$125 - 32 = 93$$

$$k) 1^3 + 14 + 1$$

$$1 + 14 + 1 = 16$$

$$l) 216 - 49 - (10)^{14}: (10)^{12}$$

$$216 - 49 - 10^2$$

$$216 - 49 - 100$$

$$67$$

$$m)$$

$$\begin{aligned} & \frac{(3^4 \cdot 3^{-2})}{3^2} + \frac{2^5}{2^3} - (-3)^2 + \left(\frac{1}{3}\right)^{-2} \\ & \frac{3^{4-2}}{3^2} + 2^{5-3} - 9 + 3^2 \\ & \frac{3^2}{3^2} + 4 - 9 + 9 \\ & 1 + 4 - 9 + 9 = 5 \end{aligned}$$

n)

$$\begin{aligned} & \left(\frac{4^3}{4^5}\right) \cdot 4^2 + (-2)^4 - \frac{3^5}{3^2} + \left(\frac{1}{2}\right)^{-3} \\ & 4^{3-5} \cdot 4^2 + 16 - 3^{5-2} + 2^3 \\ & 4^{-2} \cdot 4^2 + 16 - 27 + 8 \\ & 1 + 16 - 27 + 8 = -2 \end{aligned}$$

5)

$$x^4 - 3x^2y^2 - y^3$$

$$\text{com } x = -2 \text{ e } y = -3$$

$$\begin{aligned} & (-2)^4 - 3(-2)^2(-3)^2 - (-3)^3 \\ & 16 - 3 \cdot 4 \cdot 9 - (-27) \\ & 16 - 108 + 27 \\ & -65 \end{aligned}$$

6)

Metade do bolo:

$$\frac{1}{2}$$

Um terço do bolo:

$$\frac{1}{3}$$

Diferença:

$$\frac{1}{2} - \frac{1}{3} = \frac{3-2}{6} = \frac{1}{6}$$

Metade da diferença:

$$\frac{1}{6} \div 2 = \frac{1}{12}$$

Resposta:  $\boxed{\frac{1}{12}}$

7)

$$y = \frac{3^8 \cdot 9^{-2} \cdot 27^{-1}}{81}$$

Transformando:

$$\begin{aligned} 9^{-2} &= (3^2)^{-2} = 3^{-4} \\ 27^{-1} &= (3^3)^{-1} = 3^{-3} \\ 81 &= 3^4 \end{aligned}$$

Então:

$$\begin{aligned} y &= \frac{3^8 \cdot 3^{-4} \cdot 3^{-3}}{3^4} \\ &= 3^{8-4-3-4} \\ &= 3^{-3} \end{aligned}$$

Resposta:  $\boxed{3^{-3}}$

8)

$$y = \frac{2^{12} \cdot 4^{-2} \cdot 8^{-1}}{16}$$

Transformando:

$$\begin{aligned} 4^{-2} &= (2^2)^{-2} = 2^{-4} \\ 8^{-1} &= (2^3)^{-1} = 2^{-3} \\ 16 &= 2^4 \end{aligned}$$

Então:

$$\begin{aligned}y &= \frac{2^{12} \cdot 2^{-4} \cdot 2^{-3}}{2^4} \\ &= 2^{12-4-3-4} \\ &= 2^1\end{aligned}$$

Resposta:  $\boxed{2}$

9)

a)

$$\begin{aligned}&\sqrt{62 + \sqrt{2 + \sqrt{3 + \sqrt{1}}}} \\ &\sqrt{1} = 1 \\ &\sqrt{3 + 1} = \sqrt{4} = 2 \\ &\sqrt{2 + 2} = \sqrt{4} = 2 \\ &\sqrt{62 + 2} = \sqrt{64} = 8\end{aligned}$$

b)

$$\begin{aligned}&\sqrt{79 + \sqrt{2 + \sqrt{3 + \sqrt{1}}}} \\ &\sqrt{1} = 1 \\ &\sqrt{3 + 1} = 2 \\ &\sqrt{2 + 2} = 2 \\ &\sqrt{79 + 2} = \sqrt{81} = 9\end{aligned}$$

**Gabarito 5**

1)

**Encontrando P**

$$P \cdot (+4) = (-8) \cdot (-9)$$

Primeiro:

$$(-8) \cdot (-9) = 72$$

Então:

$$4P = 72$$
$$P = \frac{72}{4} = 18$$

### **Encontrando A**

$$A \cdot [(+8) - (+7)] = -5$$

Dentro do colchete:

$$8 - 7 = 1$$

Então:

$$A \cdot 1 = -5$$
$$A = -5$$

### **Encontrando Z**

$$5 \cdot (Z - 7) = -40$$
$$Z - 7 = \frac{-40}{5}$$
$$Z - 7 = -8$$
$$Z = -1$$

### **Calculando**

$$(P + A + Z) + P - A - Z$$

Substituindo:

$$(18 + (-5) + (-1)) + 18 - (-5) - (-1)$$

Primeiro parêntese:

$$18 - 5 - 1 = 12$$

Depois:

$$12 + 18 + 5 + 1 \\ = 36$$

**Resposta:**  $\boxed{36}$

2)

Temos:

$$T = (-1) \cdot [(-2) - (-4)]$$

Dentro do colchete:

$$-2 + 4 = 2$$

Então:

$$T = (-1) \cdot 2 = -2$$

Agora V:

$$V = 6 + [(-3) \cdot (+3)]$$

$$(-3) \cdot (+3) = -9$$

$$V = 6 + (-9) = -3$$

Calculando:

$$(2T - 3V) : 5$$

Substituindo:

$$[2(-2) - 3(-3)] \div 5$$

$$(-4) - (-9)$$

$$-4 + 9 = 5$$

$$5 \div 5 = 1$$

**Resposta:**  $\boxed{1}$

3A)

$$\sqrt{0,444\dots} \cdot \frac{3}{4} - 4 + 0,25$$

Sabemos:

$$0,444\dots = \frac{4}{9}$$

Então:

$$\sqrt{\frac{4}{9}} = \frac{2}{3}$$

Agora:

$$\begin{aligned} \frac{2}{3} \cdot \frac{3}{4} &= \frac{6}{12} = \frac{1}{2} \\ \frac{1}{2} - 4 + 0,25 & \\ 0,5 - 4 + 0,25 & \\ -3,25 & \end{aligned}$$

**Resposta:** -3,25

**3B)**

$$(1,444\dots + 0,5) : \frac{7}{10}$$

Sabemos:

$$1,444\dots = \frac{13}{9}$$

e

$$0,5 = \frac{1}{2}$$

Somando:

$$\frac{13}{9} + \frac{1}{2}$$

$$\text{MMC} = 18$$

$$\frac{26}{18} + \frac{9}{18} = \frac{35}{18}$$

Agora dividir por:

$$\frac{35}{18} \div \frac{7}{10}$$

Multiplica pelo inverso:

$$\frac{35}{18} \cdot \frac{10}{7}$$

Simplificando:

$$\begin{aligned} 35 \div 7 &= 5 \\ \frac{5 \cdot 10}{18} &= \frac{50}{18} = \frac{25}{9} \end{aligned}$$

**Resposta:**  $\boxed{\frac{25}{9}}$

**3C)**

$$\frac{0,888\dots - (-3)^{-2}}{(-1)^3 + 0,888\dots}$$

Sabemos:

$$0,888\dots = \frac{8}{9}$$

e:

$$(-3)^{-2} = \frac{1}{(-3)^2} = \frac{1}{9}$$

Numerador:

$$\frac{8}{9} - \frac{1}{9} = \frac{7}{9}$$

Denominador:

$$\begin{aligned} (-1)^3 &= -1 \\ -1 + \frac{8}{9} \\ -\frac{9}{9} + \frac{8}{9} &= -\frac{1}{9} \end{aligned}$$

Então:

$$\frac{\frac{7}{9}}{-\frac{1}{9}} = \frac{7}{9} \cdot \frac{9}{-1} = -7$$

**Resposta:**  $\boxed{-7}$

**3D)**

$$\left(2,333\dots\right)^{-2} + \frac{(3)^{14}}{27^3}$$

Sabemos:

$$2,333\dots = \frac{7}{3}$$

Então:

$$\left(\frac{7}{3}\right)^{-2} = \left(\frac{3}{7}\right)^2 = \frac{9}{49}$$

Agora:

$$\begin{aligned} 27^3 &= (3^3)^3 = 3^9 \\ \frac{3^{14}}{3^9} &= 3^5 = 243 \end{aligned}$$

Somando:

$$\begin{aligned} 243 + \frac{9}{49} \\ = \frac{11907 + 9}{49} \\ = \frac{11916}{49} \end{aligned}$$

**Resposta:**  $\boxed{\frac{11916}{49}}$

**3E)**

$$\frac{0,555\dots - \sqrt{0,25}}{\left(\frac{2}{3}\right)^2 \cdot 10^{-1}}$$

Sabemos:

$$0,555\dots = \frac{5}{9}$$

e:

$$\sqrt{0,25} = 0,5 = \frac{1}{2}$$

Numerador:

$$\frac{5}{9} - \frac{1}{2}$$

MMC = 18

$$\frac{10}{18} - \frac{9}{18} = \frac{1}{18}$$

Denominador:

$$\left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

$$10^{-1} = \frac{1}{10}$$

$$\frac{4}{9} \cdot \frac{1}{10} = \frac{4}{90} = \frac{2}{45}$$

Agora:

$$\frac{1/18}{2/45}$$

$$\frac{1 \cdot 45}{18 \cdot 2}$$

$$= \frac{45}{36} = \frac{5}{4}$$

**Resposta:**  $\boxed{\frac{5}{4}}$

**3F)**

$$\frac{0,333... + \frac{5^0}{4} + \frac{2}{3}}{\frac{1}{2} + 2^{-1} + 2^3}$$

Sabemos:

$$0,333... = \frac{1}{3}$$

$$5^0 = 1$$

Então:

$$\frac{1}{4}$$

Numerador:

$$\frac{1}{3} + \frac{1}{4} + \frac{2}{3}$$

$$\frac{1}{3} + \frac{2}{3} = 1$$

$$1 + \frac{1}{4} = \frac{5}{4}$$

Denominador:

$$2^{-1} = \frac{1}{2}$$
$$\frac{1}{2} + \frac{1}{2} + 8$$
$$1 + 8 = 9$$

Então:

$$\frac{5/4}{9} = \frac{5}{36}$$

**Resposta:**  $\boxed{\frac{5}{36}}$

**3G)**

$$0,11 + \frac{1}{5} + 1,222\dots$$

Sabemos:

$$0,11 = \frac{11}{100}$$
$$1,222\dots = \frac{11}{9}$$

Então:

$$\frac{11}{100} + \frac{1}{5} + \frac{11}{9}$$

MMC = 900

$$\frac{99}{900} + \frac{180}{900} + \frac{1100}{900}$$
$$= \frac{1379}{900}$$

**Resposta:**  $\frac{1379}{900}$